



Oxford Cambridge and RSA

AS Level Further Mathematics B (MEI)

Y415 Mechanics b

Sample Question Paper

UPDATED August 2022

Please note that Y415 Mechanics b has now been withdrawn from AS Level Further Mathematics B (MEI) and will no longer be assessed. The final assessment opportunity for this unit was June 2022.

For further information please see the Subject Update [here](#).

AS Level Further Mathematics B (MEI)

Y415 Mechanics b

Sample Question Paper

Version 3

Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes

You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

You may use:

- a scientific or graphical calculator

INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.

INFORMATION

- The total number of marks for this paper is **60**.
- The marks for each question are shown in brackets [].
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **8** pages.

Answer **all** the questions.

- 1** A particle, P, has velocity $v \text{ m s}^{-1}$ at time t seconds given by $\mathbf{v} = \begin{pmatrix} 6(t^2 - 3t + 2) \\ 2(1 - t) \\ 3(t^2 - 1) \end{pmatrix}$, where $0 \leq t \leq 3$.

(i) Show that there is just one time at which P is instantaneously at rest and state this value of t . **[3]**

P has a mass of 5 kg and is acted on by a single force \mathbf{F} N.

(ii) Find \mathbf{F} when $t = 2$. **[4]**

(iii) Find an expression for the position, \mathbf{r} m, of P at time t s, given that $\mathbf{r} = \begin{pmatrix} -5 \\ 2 \\ 6 \end{pmatrix}$ when $t = 0$. **[5]**

- 2** A smooth wire is bent to form a circle of radius 2.5 m; the circle is in a horizontal plane. A small ring of mass 0.2 kg is travelling round the wire.

(i) At one instant the ring is travelling at an angular speed of 120 revolutions per minute.

(A) Calculate the angular speed in radians per second. **[1]**

(B) Calculate the component towards the centre of the circle of the force exerted on the ring by the wire. **[4]**

(ii) Why must the contact between the wire and the ring be smooth if your answer to part (i) (B) is also the total horizontal component of the force exerted on the ring by the wire? **[1]**

- 3** A young woman wishes to make a bungee jump. One end of an elastic rope is attached to her safety harness. The other end is attached to the bridge from which she will jump.

She calculates that the stretched length of the rope at the bottom of her motion should be 20 m, she knows that her weight is 576 N and the stiffness of the elastic rope is 90 N m^{-1} . She has to calculate the unstretched length of rope required to perform the jump safely.

She models the situation by assuming the following.

- The rope is of negligible mass.
- Air resistance may be neglected.
- She is a particle.
- She moves vertically downwards from rest.
- Her starting point is level with the fixed end of the rope.
- The length she calculates for the rope does not include any extra for attaching the ends.

(i) (A) Show that the greatest extension of the rope, X , satisfies the equation $X^2 = 256$. **[3]**

(B) Hence determine the natural length of rope she needs. **[2]**

(ii) To remain safe she wishes to be sure that, if air resistance is taken into account, the stretched length of the rope of natural length determined in part **(i)** will not be more than 20 m. Advise her on this point. **[1]**

- 4 Two uniform circular discs with the same radius, A of mass 1 kg and B of mass 5.25 kg, slide on a smooth horizontal surface and collide obliquely with smooth contact.

Fig. 4 gives information about the velocities of the discs just before and just after the collision.

- The line XY passes through the centres of the discs at the moment of collision
- The components parallel and perpendicular to XY of the velocities of A are shown
- Before the collision, B is at rest and after it is moving at 2 m s^{-1} in the direction XY

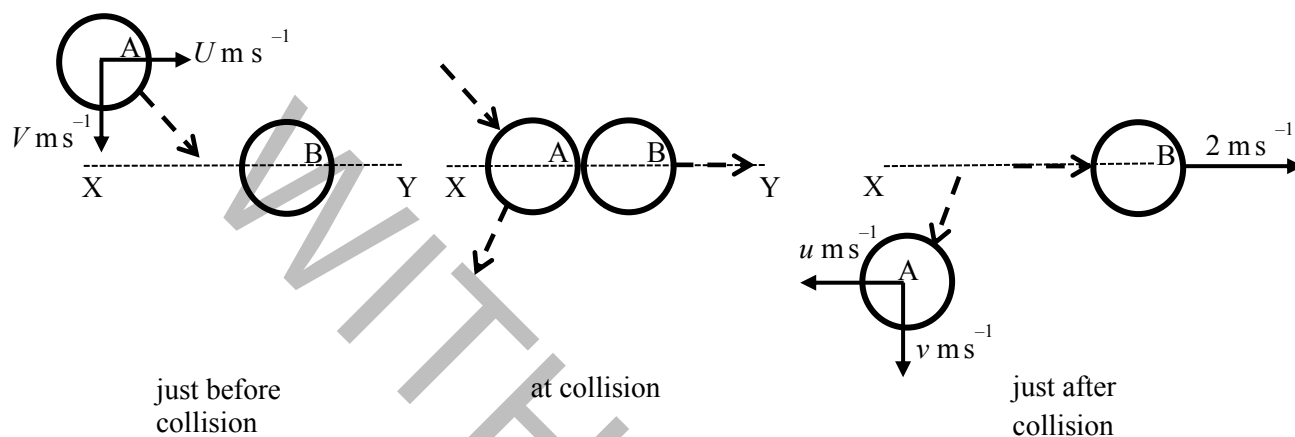


Fig. 4

The coefficient of restitution between the two discs is $\frac{2}{3}$.

- (i) Find the values of U and u . [5]

- (ii) What information in the question tells you that $v = V$? [1]

The speed of disc A before the collision is 8.5 m s^{-1} .

- (iii) Find the speed of disc A after the collision. [2]

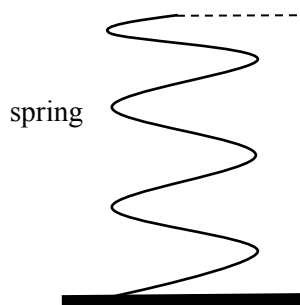


Fig. 5.1

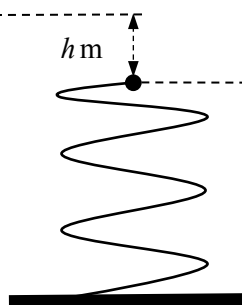


Fig. 5.2

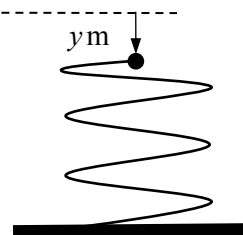


Fig. 5.3

Fig. 5.1 shows a vertical light elastic spring. It is fixed to a horizontal table at one end. Fig 5.2 shows the spring with a particle of mass m kg attached to it at the other end. The system is in equilibrium when the spring is compressed by a distance h m.

- (i) Find an expression for the stiffness of the spring, k N m⁻¹, in terms of m , h and g . [1]

The particle is pushed down a further distance from the equilibrium position and released from rest. At time t seconds, the displacement of the particle from the equilibrium position of the system is y m in the downward direction, as shown in Fig. 5.3. You are given that $|y| \leq h$.

- (ii) Show that the motion of the particle is modelled by the differential equation $\frac{d^2 y}{dt^2} + \frac{gy}{h} = 0$. [4]

- (iii) Find an expression for the period of the motion of the particle. [1]

- (iv) Would the model for the motion of the particle be valid for large values of m ? Justify your answer. [1]

6 In this question you must show detailed reasoning.

As shown in Fig. 6.1, the region R is bounded by the lines $x = 1$, $x = 2$, $y = 0$ and the curve $y = 2x^2$ for $1 \leq x \leq 2$. A uniform solid of revolution, S , is formed when R is rotated through 360° about the x -axis.

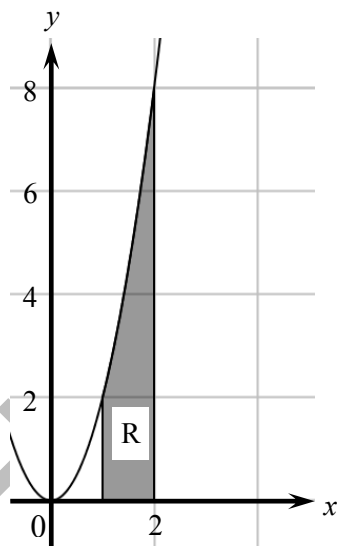


Fig. 6.1

- (i) Show that the volume of S is $\frac{124\pi}{5}$. [3]
- (ii) Show that the distance of the centre of mass of S from the centre of its smaller circular plane surface is $\frac{43}{62}$. [5]

Fig. 6.2 shows S placed so that its smaller circular plane surface is in contact with a slope inclined at α° to the horizontal. S does not slip but is on the point of tipping.

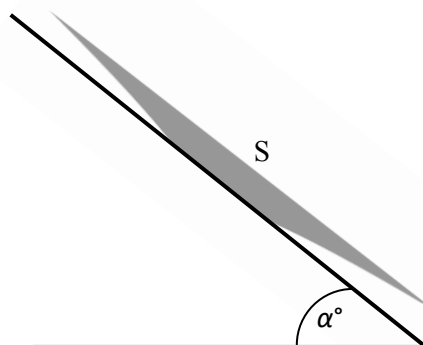


Fig. 6.2

- (iii) Find the value of α , giving your answer in degrees correct to 3 significant figures. [4]

- 7 A plane is inclined at 30° above the horizontal. A particle is projected up the plane from a point C on the plane with a velocity of 14 m s^{-1} at 40° above a line of greatest slope of the plane. The particle hits the plane at D. See Fig. 7.

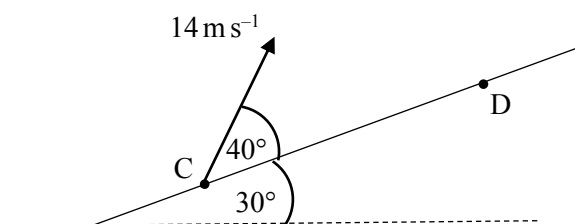


Fig. 7

- (i) Using the standard model for projectile motion, show that the time of flight, T , is given by

$$T = \frac{28 \sin 40^\circ}{g \cos 30^\circ} \quad [5]$$

- (ii) Calculate the distance CD. [4]

END OF QUESTION PAPER

WITHDRAWN

Copyright Information:

OCR is committed to seeking permission to reproduce all third-party content that it uses in the assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements booklet. This is produced for each series of examinations and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity.

For queries or further information please contact OCR, The Triangle Building, Shaftesbury Road, Cambridge CB2 8EA

OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.