Further Mechanics 2 Mark Scheme (Section B)

Question	Scheme	Marks	AOs
5 (a)	Multiply out and differentiate wrt t	M1	1.1b
	$v = 3t^2 - 16t + 20 \Rightarrow a = 6t - 16$	A1	1.1b
		(2)	
(b)	Multiply out and integrate wrt t	M1	1.1b
	$s = \int 3t^2 - 16t + 20 \mathrm{d}t = t^3 - 8t^2 + 20t (+C)$	A1	1.1b
	$t = 0, s = 0 \Rightarrow C = 0$ $t = 2, s = 8 - 32 + 40 = 16$	A1	1.1b
		(3)	
(c)	$s = 0 \Rightarrow t^3 - 8t^2 + 20t = 0$ and $t \neq 0 \Rightarrow t^2 - 8t + 20 = 0$	M1	2.1
	Explanation to show that $t^2 - 8t + 20 > 0$ for all t.	M1	2.4
	So $s = 0$ has no non-zero solutions, so s is never zero again, so never returns to O *	A1*	3.2a
		(3)	
			(8 marks)

Notes:

(a)
M1: For multiplying out and differentiating (powers decreasing by 1)
A1: For a correct expression for a

(b)
M1: For multiplying out and integrating (powers increasing by 1)
A1: For a correct expression for s with or without C
A1: For $C = 0$ and correct final answer

(c)
M1: For equating their s to 0 and producing a quadratic
M1: For clear explanation that $t^2 - 8t + 20 > 0$ for all t (e.g. completing the square or another complete method)
A1*: For a correct conclusion in context

Question	Scheme	Marks	AOs
6(a)	$\cos\alpha = \frac{4}{5}$ or $\sin\alpha = \frac{3}{5}$	B1	1.1b
	$r = 4a\sin\alpha$	B1	1.1b
	Resolving vertically	M1	3.1b
	$T_1\cos\alpha - T_2\sin\alpha = mg$	A1	1.1b
	Resolving horizontally	M1	3.1b
	$T_1\sin\alpha + T_2\cos\alpha = mr\omega^2$	A1	1.1b
	$T_1\sin\alpha + T_2\cos\alpha = mr\omega^2$	A1	1.1b
	Solving for either tension	M1	2.1
	$T_1 = \frac{4m}{25}(9a\omega^2 + 5g)$ *	A1*	1.1b
	$T_2 = \frac{3m}{25}(16a\omega^2 - 5g)$ *	A1*	1.1b
		(10)	
(b)	$\frac{4m}{25}(9a\omega^2 + 5g) < 4mg$	M1	2.1
	$\frac{3m}{25}(16a\omega^2 - 5g) > 0$	M1	2.1
	$\omega > \sqrt{\frac{5g}{16a}}$ or $\omega < \sqrt{\frac{20g}{9a}}$	A1	2.2a
	$S = \frac{2\pi}{\omega}$	M1	1.1b
	$3\pi\sqrt{\frac{a}{5g}} < S < 8\pi\sqrt{\frac{a}{5g}}$ *	A1*	1.1b
		(5)	
(c)	String being light implies that the tension is constant in both portions of the string	B1	3.5b
		(1)	
			(16 marks)

Notes:

(a)
B1: For correct trig. ratio seen
B1: For a correct radius expression seen
M1: For resolving vertically with correct no. of terms and tensions resolved
A1: For a correct equation
M1: For resolving horizontally with correct no. of terms and tensions resolved
A1A1: For a correct equation
M1: For solving their two equations to find either tension
A1*: For the given answer
A1*: For the given answer

Question 6 notes continued:
(b) **M1:** For use of $T_1 < 4mg$ **M1:** For using $T_2 > 0$ **A1:** For a correct inequality (either) for ω **M1:** For use of $S = \frac{2\pi}{\omega}$ with either critical value **A1*:** For given answer
(c) **B1:** For a clear explanation

Question	Scheme	Marks	AOs
7(a)	Rel. Mass: 2 5 1 8	B1	1.2
	y : 2 0.5 1.5 $\overline{y}$	B1	1.2
	x : 0.5 2.5 4.5 $\overline{x}$	B1	1.2
	$(2 \times 2) + (5 \times 0.5) + (1 \times 1.5) = 8\overline{y}$	M1	2.1
	$\overline{y} = 1$ *	A1*	1.1b
	$(2 \times 0.5) + (5 \times 2.5) + (1 \times 4.5) = 8\overline{x}$	M1	2.1
	$\overline{x} = 2.25$	A1	1.1b
		(7)	
(b)	Use of correct strategy to solve the problem by use of 'moments equation'	M1	3.1b
	$(8 \times 2.25) - (2\pi r^2 \times 0.5) = (8 - 2\pi r^2)2.5$	A1ft	1.1b
	Solving for r	M1	1.1b
	$r = \frac{1}{\sqrt{2\pi}} = 0.399$	A1	1.1b
		(4)	
(c)	Since $\overline{y}$ for original plate is 1, holes must be symmetrically placed about the line $y = 1$	B1	2.4
	$a = 1.5$	B1	2.2a
		(2)	
(d)	Use of tan from an appropriate triangle	M1	1.1a
	$\tan\alpha = \frac{2}{1.5} = \frac{4}{3}$	A1ft	1.1b
	$\alpha = 53.1^o$	A1	1.1b
		(3)	
			(16 marks)

Notes:

(a)
B1: For correct relative masses
B1: For correct y values
B1: For correct x values
M1: For a moments equation, correct no. of terms, condone sign errors
A1*: For a correct given answer (1)
M1: For a moments equation, correct no. of terms
A1: For 2.25

(b)
M1: For a moments equation, correct no. of terms, condone sign errors
A1ft: For a correct equation, follow through on their $\overline{x}$
M1: For solving for r
A1: For 0.399 or 0.40

Question 7 notes continued:
(c) **B1:** For consideration of symmetry about $y = 1$ **B1:** For $a = 1.5$
(d) **M1:** For use of tan from an appropriate triangle **A1ft:** For a correct equation, follow through on their a **A1:** For a correct angle