

AS Level Further Mathematics B (MEI) Y410 Core Pure

Sample Question Paper

Version 2.1

Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes



You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

You may use:

• a scientific or graphical calculator



INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION

- The total number of marks for this paper is **60**.
- The marks for each question or part question are shown in brackets [].
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

Answer all the questions.

2

The complex number z₁ is 1+ i and the complex number z₂ has modulus 4 and argument π/3.
 (i) Express z₂ in the form a + bi, giving a and b in exact form. [2]
 (ii) Express z₂/z₁ in the form c + di, giving c and d in exact form. [2]

- 2 (i) Describe fully the transformation represented by the matrix $\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$.
 - (ii) A triangle of area 5 square units undergoes the transformation represented by the matrix $\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$. Explaining your reasoning, find the area of the image of the triangle following this transformation. [2]

[2]

3 (i) Write down, in complex form, the equation of the locus represented by the circle in the Argand diagram shown in Fig. 3. [2]





(ii) On the copy of Fig. 3 in the Printed Answer Booklet mark with a cross any point(s) on the circle for which $\arg(z-2i) = \frac{\pi}{4}$. [2] 4 (i) Find the coordinates of the point where the following three planes intersect. Give your answers in terms of *a*.

$$\begin{array}{rcl}
 x - 2y - & z = & 6 \\
 3x + & y + 5z = -4 \\
 -4x + 2y - 3z = & a
 \end{array}$$
[4]

(ii) Determine whether the intersection of the three planes could be on the *z*-axis. [2]

5 The cubic equation
$$x^3 - 4x^2 + px + q = 0$$
 has roots α , $\frac{2}{\alpha}$ and $\alpha + \frac{2}{\alpha}$.

Find

- the values of the roots of the equation,
- the value of *p*.

[7]

[1]

6 (i) Show that, when
$$n = 5$$
, $\sum_{r=n+1}^{2n} r^2 = 330$.

- (ii) Find, in terms of *n*, a fully factorised expression for $\sum_{r=n+1}^{2n} r^2$. [4]
- 7 The plane Π has equation 3x 5y + z = 9.
 - (i) Show that Π contains
 - the point (4,1,2)

and

• the vector
$$\begin{pmatrix} 1\\1\\2 \end{pmatrix}$$
. [4]

(ii) Determine the equation of a plane which is perpendicular to Π and which passes through (4,1,2). [3]

8 In this question you must show detailed reasoning.

- (i) Explain why all cubic equations with real coefficients have at least one real root. [2]
- (ii) Points representing the three roots of the equation $z^3 + 9z^2 + 27z + 35 = 0$ are plotted on an Argand diagram.

Find the exact area of the triangle which has these three points as its vertices. [7]

9 You are given that matrix $\mathbf{M} = \begin{pmatrix} -3 & 8 \\ -2 & 5 \end{pmatrix}$.

(i) Prove that, for all positive integers n, $\mathbf{M}^n = \begin{pmatrix} 1-4n & 8n \\ -2n & 1+4n \end{pmatrix}$. [6]

(ii) Determine the equation of the line of invariant points of the transformation represented by the matrix M.

It is claimed that the answer to part (ii) is also a line of invariant points of the transformation represented by the matrix \mathbf{M}^n , for any positive integer *n*.

(iii)	Explain <i>geometrically</i> why this claim is true.	[2]
(iv)	Verify <i>algebraically</i> that this claim is true.	[3]

END OF QUESTION PAPER

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