Questi	on Scheme	Marks	AOs
6	$\begin{pmatrix} P & Q & R & S & T & X \\ A & 32 & 32 & 35 & 34 & 33 & 40 \\ B & 28 & 35 & 31 & 37 & 40 & 40 \\ C & 35 & 29 & 33 & 36 & 35 & 40 \\ D & 36 & 30 & 34 & 33 & 35 & 40 \\ E & 30 & 31 & 29 & 37 & 36 & 40 \\ F & 29 & 28 & 32 & 31 & 34 & 40 \end{pmatrix}$	B1	1.1b
	Reducing rows and then columns $\begin{pmatrix} P & Q & R & S & T & X \\ A & 0 & 0 & 3 & 2 & 1 & 8 \end{pmatrix}$ $\begin{pmatrix} P & Q & R & S & T & X \\ A & 0 & 0 & 3 & 0 & 0 & 0 \end{pmatrix}$		
	$ \begin{bmatrix} A & 0 & 0 & 3 & 2 & 1 & 8 \\ B & 0 & 7 & 3 & 9 & 12 & 12 \\ C & 6 & 0 & 4 & 7 & 6 & 11 \\ D & 6 & 0 & 4 & 3 & 5 & 10 \\ E & 1 & 2 & 0 & 8 & 7 & 11 \end{bmatrix} $ then $ \begin{bmatrix} A & 0 & 0 & 3 & 0 & 0 & 0 \\ B & 0 & 7 & 3 & 7 & 11 & 4 \\ C & 6 & 0 & 4 & 5 & 5 & 3 \\ D & 6 & 0 & 4 & 1 & 4 & 2 \\ E & 1 & 2 & 0 & 6 & 6 & 3 \end{bmatrix} $	M1 A1	1.1b 1.1b
	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	M1	1.1b
	$ \begin{pmatrix} P & Q & R & S & T & X \\ A & 1 & 1 & 3 & 0 & 0 & 0 \\ B & 0 & 7 & 2 & 6 & 10 & 3 \\ C & 6 & 0 & 3 & 4 & 4 & 2 \end{pmatrix} $ followed by $ \begin{pmatrix} P & Q & R & S & T & X \\ A & 2 & 2 & 3 & 1 & 0 & 0 \\ B & 0 & 7 & 1 & 6 & 9 & 2 \\ C & 6 & 0 & 2 & 4 & 3 & 1 \end{pmatrix} $	A1ft M1	1.1b 1.1b
	$ \begin{vmatrix} D & 6 & 0 & 3 & 0 & 4 & 1 \\ E & 2 & 3 & 0 & 6 & 6 & 3 \\ F & 1 & 0 & 3 & 0 & 4 & 3 \end{vmatrix} $ $ \begin{vmatrix} D & 6 & 0 & 2 & 0 & 3 & 0 \\ E & 3 & 4 & 0 & 7 & 6 & 3 \\ F & 1 & 0 & 2 & 0 & 3 & 2 \end{vmatrix} $	A1ft A1	1.1b 1.1b
	A – T, B – P, C – Q, (D – ), E – R, F – S	Al	2.2a
<b>N - + - - -</b>		(9 n	narks)
M1: A1: M1:	cao – introducing a dummy task and appropriate value Simplifying the initial matrix by reducing rows and then columns cao Develop an improved solution – need to see Double covered +e; one unco one single covered unchanged. 4 lines to 5 lines needed	vered –e ;	and
M1: A1ft: A1: A1:	It on their previous table – no errors Finding the optimal solution – need to see one double covered +e; one uncome single covered unchanged. 5 lines needed to 6 lines needed (so getting able) It on their previous table – no errors eso on final table (so must have scored all previous marks) eso – this mark is dependent on all M marks being awarded – to deduce the allocation from the location of zeros in the table	g to the opt	

## **Decision Mathematics 2 Mark Scheme (Section B)**

Questio	n Scheme	Marks	AOs
7(a)	16, 22, 29	B1	1.1b
		(1)	
(b)	$u_{n+1} = u_n + n + 1$	B1	3.3
		(1)	
(c)	As $u_{n+1} = u_n + p(n) \implies u_n = \lambda n^2 + \mu n + \phi$ and attempt to solve with $n = 1, 2, 3$	M1	1.1b
	$u_n = \frac{1}{2}n(n+1) + 1$	A1	1.1b
	2 20 101 (regions)	A1ft	1.1b
		(3)	
		(5 n	narks)
Notes:			
(a) B1: ca	0		
(b) B1: T	anslating problem to mathematical model - correct recurrence relation r	needed	
(c) M1: A A1: ca	n attempt to solve the recurrence relation to determine maximum numbe	er of regior	15
Alft: S	Substitution of $n = 200$ into their quadratic $u_n$ expression		

Question	Scheme	Marks	AOs
<b>8</b> (a)	Corridors must be one-way	B1	3.4
		(1)	
(b)	e.g. $55 + x + 40 = 63 + 54 + 24$ or $7 + y = 54 + 5$	M1	2.4
	x = 46	A1	1.1b
	<i>y</i> = 52	A1	1.1b
		(3)	1 11
(c)	(i) SACET (= 5) SDFET (= 5)	M1 A1	1.1b 1.1b
	(ii) Students must choose SACET, as they cannot travel from F to E	A1	2.2a
		(3)	
(d)	A 40 $C60$ $20$ $35$ $12$ $6351$ $21$ $D$ $5$ $0$ $24$ $T40$ $B$ $19$ $F$	B1	1.1b
		(1)	
(e)	Use of max-flow min-cut theorem	M1	2.1
	Identification of cut through AC, DC, DE, (EF), FT = 151 value of flow = 151	A1	3.1a
	Therefore it follows that flow is optimal	A1	2.2a
		(3)	
(f)	Consider increasing capacity of arcs in minimum cut	B1	2.1
	<ul> <li>Explanation based on a valid argument, such as:</li> <li>increasing the capacity of any arc other than FT would not increase the flow by more than 1, as total capacity directly in to T is only 152</li> <li>increasing the capacity on FT could increase the total flow by 16 (increased flow along SAD, SD and SBD could all be directed through DF to F)</li> </ul>	B1	2.4
	Therefore school should choose to widen FT, which could increase the flow through the network by 16	B1	2.2a
		(3)	
		(14 n	narks)

Ques	tion 8 notes:
(a)	
B1:	Explanation of assumption to use this model
(b)	
M1:	Either a correct equation, or explanation that flow in = flow out
A1:	cao
A1:	cao
(c)	
M1:	One flow augmenting route found from S to T
A1:	Two correct flow augmenting routes 5+
A1:	Deduce that SACET must be used as students cannot travel from F to E as route is one-way
(d)	
<b>B1:</b>	A consistent flow pattern = 151
(e)	
M1:	Constructing argument based on max-flow min-cut theorem
A1:	Use appropriate process of finding a minimum cut – cut + value correct
A1:	Correct deduction that the flow is maximal
(f)	
B1	Constructing an argument based on arcs in the minimum cut
<b>B</b> 1	Detailed explanation as to why choosing anything other than FT does not help
B1	Correct deduction and correct increase in flow of 16

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Question	Scheme	Marks	AOs
9(a)	Row minima: 1, 2 max is 2	M1	1.1b
	Column maxima: 4, 4, 3 min is 3	Al	1.1b
	Row maximin (2) $\neq$ Column minimax (3) so not stable	Al	2.4
		(3)	
(b)	Let A play strategy 1 with probability $p$ and strategy 2 with probability 1- $p$ , and using this to get at least one equation in $p$	M1	3.3
	Then if B plays strategy 1, A's gains are $4p + 2(1-p) = 2p + 2$	A1	1.1b
	If B plays strategy 2, A's gains are $p + 4(1-p) = 4 - 3p$ If B plays strategy 3, A's gains are $2p + 3(1-p) = 3 - p$	Al	1.1b
	6 - 1 = 6		
	5 5		
	4 - 2p + 2 - 4		
	3 - p - 3		
	2 2		
	1 - 4 - 3p - 1		
	p = 0 $p = 1$		
	-1-		
	Intersection of $2p + 2$ and $3 - p$ occurs where $p = \frac{1}{3}$	dM1	1.1b
		A1ft	1.1b
	Therefore player A should play strategy $1\frac{1}{3}$ of the time and play strategy $2\frac{2}{3}$ of the time	A1ft	3.2a
	The value of the game to player A is $2\frac{2}{3}$	A1	1.1b
		(9)	
			arks)

Question 9 notes:	
(a)	
M1:	Finding row minimums and column maximums – condone one error
A1:	Row minima and column maxima correct
A1:	Explanation involving $2 \neq 3$ and a conclusion
(b)	
M1:	Translating situation into model by defining variables and constructing at least one equation
A1:	One row correct
A1:	All three rows correct
M1:	Axes correct, at least one line correctly drawn for their expression
A1:	Correct graph
M1:	Using their probability expectation graph to find the probability by equating their two correct expressions and attempting to solve as far as $p =$
A1ft:	ft on their optimal intersection
A1ft:	Interpret their value of p in the context of the question – must refer to play, player A
A1:	cao