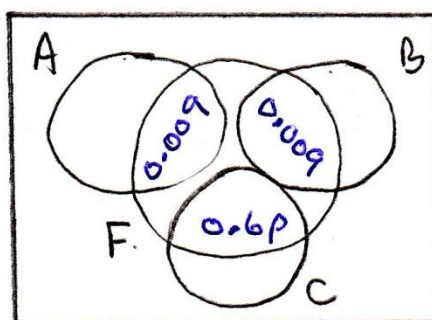
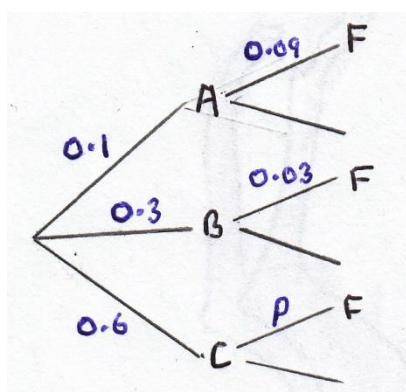


Section A: Statistics

Qu	Scheme	Marks	AO
1	(a) Positive (correlation)	B1	1.2
		(1)	
	(b) Every extra point gives £4.5(0) more on pay (o.e.)	B1	3.4
		(1)	
	(c) e.g. For points < 11 it would give pay < 0 which is ridiculous	B1	2.4
		(1)	
		(3 marks)	
Notes			
(a)	B1 for “positive”. Allow an interpretation e.g. “as points increase pay increases” is B1 Read whole answer: contradictory comments such as “positive correlation, as points increase pay decreases” scores B0		
(b)	B1 for any correct comment conveying idea of <u>£s per point</u> and including a correct value; must have idea of <u>rate</u> . Can condone missing £ sign. Accept 4.5 e.g. “every 10 points earns an <u>extra</u> (or increase) of £45” is B1 BUT “every point earns £4.5(0)” is B0 <i>doesn’t have idea of rate</i>		
(c)	B1 for a suitable comment mentioning “points” or “pay” (o.e. e.g. “amount”) or commenting on “small sample” or “range of points” used to find line <u>The following examples would score B1</u> Can say that <u>n points</u> (for $n < 10.4$) would give <u>negative pay</u> so not suitable Any comment suggesting that some jobs would end up with <u>negative pay</u> Don’t know the <u>range of points</u> used to find the <u>regression line</u> A <u>small sample of size 8</u> may not be <u>representative</u> to cover all jobs B0 for a focus on “qualifications” or “hours” worked only <u>The following examples would score B0</u> Some jobs require no (or low) skills or qualifications (<i>need negative pay</i>)		

Qu	Scheme	Marks	AO
2 (a)	[Let $p = P(F C)$ Tree diagram or some other method to find an equation for p $0.1 \times 0.09 + 0.3 \times 0.03 + 0.6 \times p = 0.06$ $p = 0.07$ i.e. <u>7%</u>	M1 A1 A1 (3)	2.1 1.1b 1.1b
(b)	e.g. $P(B \text{ and } F) = 0.3 \times 0.03 = 0.009$ but $P(B) \times P(F) = 0.3 \times 0.06 = 0.018$ These are not equal so not independent	B1 (1)	2.4
		(4 marks)	
Notes			
(a)	M1 for selecting a suitable method to find the missing probability e.g. sight of tree diagram with 0.1, 0.3, 0.6 <u>and</u> 0.09, 0.03, p suitably placed e.g. sight of VD with 0.009 for $A \cap F$ and $B \cap F$ and $0.6p$ suitably placed <u>or</u> attempt an equation with at least one correct numerical and one “ p ” product (not necessarily correct) on LHS <u>or</u> for sight of $0.06 - (0.009 + 0.009)$ (o.e. e.g. $6 - 1.8 = 4.2\%$) 1 st A1 for a correct equation for p (May be implied by a correct answer) <u>or</u> for the expression $\frac{0.06 - (0.009 + 0.009)}{0.6}$ (o.e.) 2 nd A1 for 7% (accept 0.07) Correct Ans: Provided there is no incorrect working seen award 3/3 e.g. may just see tree diagram with 0.07 for p (probably from trial and improv’)		
(b)	B1 for a suitable explanation...may talk about 2 nd branches on tree diagram and point out that $0.03 \neq 0.06$ but need some supporting calculation/words Can condone incorrect use of set notation (it is not on AS spec) provided the rest of the calculations and words are correct.		



Qu	Scheme	Marks	AO
3 (a)	Let N = the number of games Naasir wins $N \sim B(15, \frac{1}{3})$	M1	3.3
	(i) $P(N = 2) = 0.059946\dots$ awrt 0.0599	A1	1.1b
	(ii) $P(N > 5) = 1 - P(N \leq 5) = 0.38162\dots$ awrt 0.382	A1	1.1b
		(3)	
	(b) $H_0 : p = \frac{1}{3}$ $H_1 : p > \frac{1}{3}$	B1	2.5
	Let X = the number of games Naasir wins $X \sim B(32, \frac{1}{3})$	M1	3.3
	$P(X \geq 16) = 1 - P(X \leq 15) = 0.03765$ (< 0.05)	A1	3.4
	[Significant result so reject H_0 (the null model) and conclude:]	A1	3.5a
	There is evidence to support Naasir's claim (o.e.)	(4)	
		(7 marks)	
Notes			
(a)	M1 for selecting a binomial model with correct n and p Award for sight of $B(15, \frac{1}{3})$ (o.e. e.g. in words) or implied by 1 correct answer 1 st A1 for awrt 0.0599 (from a calculator). Allow 0.05995 2 nd A1 for awrt 0.382 (from a calculator)		
(b)	B1 for correctly stating both hypotheses in terms of p or π Accept $p = 0.\dot{3}$ or any exact equivalent. $H_1 : p \geq \frac{1}{3}$ is B0 M1 for selecting a suitable model to use for the test. Award for sight of $B(32, \frac{1}{3})$ (o.e. e.g. in words) or implied by 0.03765 Can also allow M1 for $P(X \leq 15) = 0.962$ or better or $P(X \leq 14) = 0.922$ or better 1 st A1 for use of the model to calculate an appropriate probability using calc. Sight of $P(X \geq 16)$ and answer awrt 0.0377		
ALT	CR May use CR so award 1 st A1 for CR of $X \geq 16$ must have seen some probabilities though: 1 of $P(X \leq 15) = 0.9623$ or $P(X \leq 14) = 0.9224$ or 0.9223 2 nd A1 for conclusion in context that there is support for Naasir's claim Must mention " <u>Naasir</u> " or " <u>his</u> " and " <u>claim</u> " or " <u>method</u> " (o.e.) <u>or</u> e.g. <u>probability</u> of <u>winning</u> a game is <u>$> \frac{1}{3}$</u> or has <u>increased</u> Dependent on M1 and 1 st A1 but can ignore hypotheses <u>but see below</u> If you see $P(X \geq 16) = 0.0376$ followed by a correct contextualised conclusion then please award A0A1		
SC	Use of 0.3 for $\frac{1}{3}$ If used 0.3 instead of $\frac{1}{3}$ in (a) and score M0A0A0 can condone use of 0.3 in (b) 1 st A1 ft needs $P(X \geq 16) = 0.0138$ <u>or</u> CR of $X \geq 15$ and sight of 1 of $P(X \geq 15) = 0.0327$ or $P(X \geq 14) = 0.0694$		

2 nd A1 as before with 0.3 instead $\frac{1}{3}$ (if appropriate)
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Qu	Scheme	Marks	AO
4 (a)	$\bar{x} = 10.2$ (2222...) awrt 10.2	B1 (1)	1.1b
(b)	$\sigma_x = 3.17$ (20227...) awrt 3.17 Sight of “knots” <u>or</u> “kn” (condone knots/s etc)	B1ft B1	1.1b 1.2
(c)	October since it is windier in the autumn <u>or</u> month of the hurricane <u>or</u> latest month in the year	B1 B1 (2)	2.2b 2.4
(d)(i)	They represent <u>outliers</u>	B1 (2)	1.2
(ii)	Y has low median so expect lowish mean (but outlier so > 7) <u>and</u> Y has big range/IQR or spread so expect larger st.dev Suggests B	M1 A1 (3)	2.4 2.2b
(8 marks)			
Notes			
NB	$\bar{x} = \frac{184}{18}$ and $\sigma_x = \sqrt{\frac{2062}{18} - \bar{x}^2}$		
(a)	B1 for $\bar{x} = 10.2$ (allow exact fraction)		
(b)	1 st B1ft allow 3.2 from a correct expr' accept $s = 3.26(3984...)$ [ft use of n/a] <u>Treating n/a as 0</u> May see $n = 31$ or $\bar{x} = 5.9354...$ which is B0 in (a) but here in (b) it gives $\sigma_x = 5.59(34...)$ or $s = 5.6858...$ (awrt 5.69) and scores 1 st B1 2 nd B1 accept kn accept in (a) or (b) (allow nautical miles/hour)		
(c)	1 st B1 choosing October but accept September. 2 nd B1 for stating that (Camborne) is windier in autumn/winter months “because it is winter/autumn/windier/colder in “month” ” Sep \leq "month" \leq Mar scores B1B1 for “month” = Sep or Oct and B0B1 for other months in range		
(d)(i)	B1 for outlier or the idea of an extreme value allow “anomaly”		
(ii)	M1 for a comment relating to location that mentions both median and mean <u>and</u> a comment relating to <u>spread</u> that mentions both range/IQR and standard deviation and leads to choosing B , C or D		

ALT	Choosing A or E is M0
	Incorrect/false statements score M0 e.g. $Q_3 = (\text{mean} + \sigma)$ or identify $Q_2 = \text{mean}$
	or Y has small spread
	Use of outliers: outlier is $(\text{mean} + 3\sigma)$ ($B = 19.9$), ($C = 18.95$), ($D = 20.2$) Must <u>see</u> at least one of these values and compare to Y 's outlier[leads to D or B]
	A1 for suitable inference i.e. B (accept D <u>or</u> B or D) M1 must be scored

Qu	Scheme	Marks	AO										
5(a)	$P(X = 4) = P(X = 2)$ so $P(X = 4) = 0.35$ $P(X = 1) = P(X = 3)$ and $P(X = 1) + P(X = 3) = 1 - 0.7$ So	M1	2.1										
	<table border="1"><tr><td>x</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>$P(X = x)$</td><td>0.15</td><td>0.35</td><td>0.15</td><td>[0.35]</td></tr></table>	x	1	2	3	4	$P(X = x)$	0.15	0.35	0.15	[0.35]	A1	1.1b
	x	1	2	3	4								
	$P(X = x)$	0.15	0.35	0.15	[0.35]								
		(2)											
	(b) Let A = number of spins that land on 4 $A \sim B(60, "0.35")$	B1ft	3.3										
	$[P(A > 30) =] \quad 1 - P(A \leq 30)$	M1	3.4										
	$= 1 - 0.99411\dots = \text{awrt } 0.00589$	A1	1.1b										
		(3)											
	(c) $Y - X \leq 4 \Rightarrow \frac{12}{X} - X \leq 4$ or $12 - X^2 \leq 4X$ (since $X > 0$) o.e.	M1	3.1a										
i.e. $0 \leq X^2 + 4X - 12 \Rightarrow 0 \leq (X + 6)(X - 2)$ so $X \geq 2$	M1	1.1b											
$P(Y - X \leq 4) = P(X \geq 2) = 0.35 + 0.15 + 0.35 = \underline{0.85}$	A1	3.2a											
	(3)												
		(8 marks)											
Notes													
(a)	M1 for using the given information to obtain $P(X = 4)$ Award for statement $P(X = 4) = P(X = 2)$ or writing $P(X = 4) = 0.35$ A1 for getting fully correct distribution (any form that clearly identifies probs) e.g. can be list $P(X = 1) = 0.15, P(X = 3) = \dots$ etc or as a probability function $P(X = x) = \begin{cases} 0.15 & x = 1, 3 \\ 0.35 & x = 2, 4 \end{cases}$ [Condone missing $P(X = 2)$ as this is given in QP]												
(b)	B1 for selecting a suitable model, sight of $B(60, \text{their } 0.35)$ o.e. in words f.t. their $P(X = 4)$ from part (a). Can be implied by $P(A \leq 30) = \text{awrt } 0.9941$ or final answer = awrt 0.00589 M1 for using their model and interpreting "more than half" Need to see $1 - P(A \leq 30)$. Can be implied by awrt 0.00589 Can ignore incorrect LHS such as $P(A \geq 30)$ A1 for awrt 0.00589												
(c)	1 st M1 for translating the prob. problem into a <u>correct</u> mathematical inequality Just an inequality in 1 variable. May be inside a probability statement.												
ALT	Table of values: <table border="1"><tr><td>X</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Y</td><td>12</td><td>6</td><td>4</td><td>3</td></tr></table> or values of $Y - X = 11, 4, 1, -1$			X	1	2	3	4	Y	12	6	4	3
X	1	2	3	4									
Y	12	6	4	3									
	2 nd M1 for solving the inequality leading to a range of values, allow 1 or 2 slips May be a quadratic or cubic but must lead to a set of values of X or $Y - X$												
ALT	Table or values: They must state clearly which values are required Both Ms can be implied by a correct answer (or correct ft of their distb'n)												
	A1 for interpreting the inequality and solving the problem i.e. 0.85 cao												